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ABSTRACT

Problems associated with the analysis of data collected using the Solomon Four Group Design are discussed. The design includes an experimental group and a control group that have been pretested and posttested, and an experimental and a control group that have been posttested only. A sample problem is approached in three different ways. First, the data are divided into two sets (those both pretested and posttested, and those posttested only) and analyzed using a simple t, test. Second, the problem is visualized as a repeated measures design wherein the pretest is the first measure and the posttest is the second measure. Using this approach, the data can be analyzed with regression techniques. Third, if the design were seen as a six group design, a one-way lay-out or a three-way lay-out are possible. Both options are discussed, including the appropriate restrictions and multiple comparison techniques. (CM)

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Using Linear Models to Simultaneously Analyze
a Solomon Four Group Design

John D. Williams and Isadore Newman

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Solomon (1949) devised a design to control threats to design validity (Campbell and Stanley, 1966). Using the notation of Campbell and Stanley, the four groups can be diagrammed as

Ŕ	01		X .		02	
Ŗ	03			•	04	r
R		•	X		05	
R					06	-

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The four groups are respectively Group One: An experimental groups that has been pretested and posttested; Group Two: A control group that has been pretested and posttested; Group Three: An experimental group that has been posttested only; and Group Four: A control group that has been posttested only.

Campbell and Stanley state, "There is no singular statistical procedure which makes use of all six sets of observations simultaneously." (p. 24)

The Solomon Four Group Design, while very simple conceptually, can be very misleading depending upon the statistical analysis. Campbell and Stanley (1966) have a preferred approach, in which they set up a 2x2 factorial design.

Treatment

•	٠	Yes	No
Pre-	Yes	Gr1	Gr2
Test	No	Gr3	Gr4

In this design only the posttest scores are statistically analyzed. This



procedure does not allow one to control for the pretest scores in groups 1 and 2, thereby losing some power; it does however estimate the effects of treatments that are independent of individuals having a pretest and treatment pretest interaction. It also tests for the effects of pretesting, independent of treatment and pretest-treatment interaction, on posttest scores. Finally, the approach estimates the effects of pretest-treatment interaction, on posttest scores.

One of the advantages of writing specific regression models which reflect research questions is that one is less likely to have a statistical answer that is unrelated to the researcher's question of interest. The following are a variety of regression models which will reflect potential research questions that can be ascertained from the Solomon Four Group Design. It should be remembered that there is not one correct answer.

Recently, Newman, Benz, and Williams (1980) devised a way to analyze data that, by extension, might be applied to Solomon type designs. A unique property of this technique is that, the statement by Campbell and Stanley not with-Standing, a single statistical procedure can be employed which makes use of all six sets of observations simultaneously. On the other hand, the solution(s) may prove to be no more satisfactory than existing possibilities that split the data into two sets. In the end, the Solomon Four Group design may prove to be one of those recalcitrant research situations that leave the would be analysts foundered on the shoal of a simple design whose simplicity is only a deception.

consider the following research situation. Five people in each group have scores such that one experimental group has been pretested and post-tested and one experimental group has been posttested only. Two similarly tested con'rol groups are also included. Data for such a situation are



given in Table 1.

Table 1

Data for a Solomon Four Group Design

Experimental: Group One			o Two	Experimental: Group Three	Control: Group Four	
^p retest	Posttest	Pretest	Posttest	Posttest	Posttest	
		•	. ?	Ŷ		
F,	15	5	8	13	9	
7	12	4	7	10	8	
, F	10	4	8	12	6	
12	17	Ŕ	6	11	3	
6	11	6	6	14	4	

Several different approaches might be tried. One approach would be to divide the data into two sets: Groups One and Two (those who were both pretested and posttested) as one set, and the posttested only groups (Groups Three and Four) as the second set. The latter set can be simply tested by the use of the test:

t = 4/24 (p<.05).

The former data set (Groups One and Two)°can be conceived either as a repeated measures design or as a problem that can be approached through the analysis of covariance (or related techniques such as residual gain analysis).

1em

To approach the problem first as an analysis of covariance, the following variables can be defined:

/ = the criterion, or posttest score;

X₁ = the pretest score;

x₂ = 1 if the score is from the experimental group, 0 if the score is from the control group;

x₃ = 1 if the score is from the control group, 0 if the score is from the control group.



Then either of two full models can be used:

$$Y = b_1 X_1 + b_2 X_2 + b_3 X_3 + e_1,$$
 (1)

$$Y = {}^{b}_{0} + {}^{b}_{1} \times {}^{1}_{1} + {}^{b}_{2} \times {}^{2}_{2} + e_{1}.$$
 (2)

Equation 2 utilizes the unit vector in the process of generating a constant whereas equation 1 does not. Either model will yield the same R^2 value.

The restricted model-(with equation 2 as the full model) is of the form:

$$Y = L_0 + b_1 X_1 + e_2.$$
 (3)

For this data set $R_2^2 = .79379$, $R_3^2 = .42334$, $F = \frac{(.79379 - .42334)/1}{(1 - .79379)/7} = 12.58$, p<_05.

Using a Repeated Measures Approacn

If the problem is visualized as a repeated measures design wherein the pretest is the first measure and the posttest is the second measure, then the design is like the Type I design shown in Lindquist (1953) and can be achieved through a regression approach (Williams, 1974). For a regression formulation, see Table 2.

Table 2
Design Matrix for a Repeated Measures Problem

					,*											
4	Pl	P ₂	P ₃	^F 4	P ₅	P ₆	Р ₇	P ₈	• P ₉	P ₁₀	^X 1	X ₂	Х3_	X ₄	X ₅ _	
5	 1	0		0	0	0	0	0	0	0	1	0	1	0	1	
7	O	1	0	0	0	0	0	U	U	0	1	0 0 0 0	1 1	0 . 0	1	
5	0	C	1	0	0	0	0	0	0	0	1	0	1	. 0	1	
12	0	0	0	1	0	0	0	0	0	0	1	Ō	1		l	
દ)	0	0 ,	0	1	0	0	0	0	0	1 /		1	0 1	1	
15	1 -	-	0	0	۰ 0	0	0	0 Q	0	0	1	0	0	l	0	
.2	0	1	0	0	0	0	0		0	0	1	0	0	1	0	
10	0	0	1	Ŋ	0	0	0	0	0	0	1	0	0	I 1	0	
17	0	0	0	1	0	0	0	0	0	0	1	, 0	. 0	1	0	Į.
lì	0	-0	0	0	1	0	0	0	0	0	1	0	U	1	0	_
5	0	0	0	O.	0	1	0	ħ	0 0	- ⁰	0	1	1	0	0	
4	0	С	0	J	0	0	1	0		U	0	1	1	0	0	
4	0	ŋ	0	0	0	0	0	1	0	0	0 0	1	1	0 0	0 0	
Ę	0	0	0	0	0	0		0	1	0		1 1	1	0	0	
6	0	ŋ	0	0	0	0	0	0	0	1 0 ,	. 0	1	0	1	0	
3	Č	0	0	0	0	1	0	0	0	0	0	1	0	1	0	
7	Ú	0	0	0	0	0	1	0	0						0	,
8	Ũ	0	0	0	0	0	0	1	0	0	0 0	1	0 Q 0	1	0	
6 6	O _k	0	0	0	0	0	0	0 0	1	0 1	0	1	ų O	1	0	
6	0	0	0	0	0	0	0	_	_	1	U	1	U	1	U	
								ī)							

Here, Y = the criterion test score;

 P_1 thru P_{10} are binary coded person vectors (1 if the person, 0 otherwise); $X_1 = 1$ if the score comes from a person in the experimental group, 0 otherwise;

 $x_2 = 1$ if score comes from a person in the control group, 0 otherwise;

 $x_3 = 1$ if the score occurs with a pretest situation, 0 otherwise;

 $\chi_4 = 1$ if the score occurs with a posttest situation, 0 otherwise; and

 $x_5 = x_1.x_3.$

Several models can be used to generate an analysis. The use of the following is instructive:

$$Y = b_0 + b_1 P_1 + b_2 P_2 + \dots + b_9 P_9 + e_3;$$
(or alternatively, $Y = b_1 P_1 + b_2 P_2 + \dots + b_{10} P_{10} + e_3$)

$$Y = b_0 + b_1 X_1 + e_4; (5)$$

$$= b_0 + b_3 x_3 + e_5;$$
 (6)

$$Y = b_0 + b_1 X_1 + b_3 X_3 + e_6;$$
 (7)

$$Y = b_0 + b_1 x_1 + b_3 x_3 + b_5 x_5 + e_7;$$
 (8)

and

$$y = b_0 + b_1 + b_2 + b_2 + \dots + b_9 + b_{10} + b_3 + b_{11} + b_5 + e_8.$$
 (9)

For the preceding, $R_4^2 = .54297$;

$$R_5^2 = .31250;$$

$$R_6^2 = .31250;$$

$$R_7^2 = .62500;$$

$$R_{g}^{2} = .76312$$
 and $R_{g}^{2} = .93359$.

What might have occured if a-model of the following form were used?

$$Y = b_0 + b_1 p_1 + b_2 p_2 + \dots + b_9 p_9 + b_{10} x_1 + b_{11} x_3 + b_{12} x_5 + e_9$$

It would not sensibly yield $R^2 = .54297 + .70312 = 1.24609$. Such a model would fail because the effect for experimental-control is "nested" in the subject (or person) effect. To test for the experimental-control effect,

$$F = \frac{R_5^2/1}{(R_A^2 - R_5^2)/(P-1-1)} = \frac{.31250/1}{(.54297 - .31250)/(10-2)} = \frac{10.85}{4}$$

p<.05.

To test for the test-retest effect,

$$F = \frac{R_6^2/1}{(1-R_9^2)/(N-P-1-1)}$$

The interaction is tested by

$$\frac{F}{(1-R_9^2)/(N-P-1-1)} = \frac{(.70312-.62500)/1}{.06641/8} = 9.41, p<.05.$$

Note that the interaction effect can be conceptualized as actually being additional evidence for the experimental effect. The higher increases in the experimental group will show up in part as interaction for a repeated measures design.

The usual summary table for the repeated measures design can be constructed. The summary table is shown in Table 3. $^\circ$

Table 3
Summary Table for Repeated Measures Design

Junian / I	ADIC TOT TOP			
•	df	SS	MS	F
Subjects Experimental-Control error (a)	9 1 8	139.00 80.00 59.00	80.00 . 7.375	10.85
Within Subjects test-retest interaction error (b)	10 1 1 8	117.00 80.00 20.00 17.00	80.00 20.00 2.125	37.65 9.41
Total	19	256.00	:	v

Using All Six Groups Simultaneously

As the Solomon design is approached, several conceptual issues ensue. Is



this to be seen as a six group design with attendant solutions? If the researcher opts for a six group design, person vector information needs to be excluded. Indeed, this was also true in the previous section. At no time were the four groups and person vectors used simultaneously; if it were, the R² was theoretically to be 1.24609, obviously an impossibility. If a six group design is to be used, what dimensions would be appropriate? This could be considered to be a one-way lay-out, a two-way lay-out, or a three-way lay-out (but with two missing cells) only the one-way and three-way layouts are discussed here. First hypotheses with a one-way lay-out as addressed.

Consider the following variables:

v = the criterion score;

- $x_1 = 1$ if the score is a pretest score from a member of the experimental group, 0 otherwise;
- $x_2 = 1$ if the score is a posttest score from a member of the experimental group that has been pretested, 0 otherwise;
- $\chi_3 = 1$ if the score is a pretest score from a member of the control group, 0 otherwise;
- $\chi_4 = 1$ if the scoremis a posttest score from a member of the control group that was pretested, 0 otherwise;
- $x_5 = 1$ if the score is from a member of the experimental group that was <u>not</u> pretested, 0 otherwise; and
- $\chi_6 = 1$ if the score is from a member of the control group that was <u>not</u> pretested, 0 otherwise.

For the six group situation, the full model is:

$$Y = b_1 x_1 + b_2 x_2 + b_3 x_3 + b_4 x_4 + b_5 x_5 + b_6 x_6 + e_9.$$
 (10)

At least two different sets of restrictions might make sense in addressing the Solomon design. One such set would be $b_2-b_1=b_4-b_3$, which addresses the hypothesis $\overline{Y}_2-\overline{Y}_1=\overline{Y}_4-\overline{Y}_3$, as the hypothesis that the gains in the twice tested

experimental and control groups are equal; also, the second restriction is $b_5 = b_6$ as the once tested experimental groups have equal means: $\overline{Y}_5 = \overline{Y}_6$.

The first restriction can be rewritten as $b_2=b_4-b_3+b_1$: Placing these two restrictions on the Full Model:

$$Y = b_{1}X_{1} + (b_{4} - b_{3} + b_{1})X_{2} + b_{3}X_{3} + b_{4}X_{4} + b_{5}X_{5} + b_{5}X_{6} + e_{10}$$

$$Y = b_{1}(X_{1} + X_{2}) + b_{3}(X_{3} - X_{2}) + b_{4}(X_{4} + X_{2}) + b_{5}(X_{5} + X_{6}) + e_{10}.$$
(12)

Letting $D_{1} = X_{1} + X_{2}$;
$$D_{2} = X_{3} - X_{2}$$
;
$$D_{3} = X_{4} + X_{2}$$
; and
$$D_{4} = X_{5} + X_{6}$$
, the restricted model is:
$$Y = b_{1}D_{1} + b_{3}D_{2} + b_{4}D_{3} + b_{5}D_{4} + e_{10}.$$
(13)

Here, $R_{10}^{2} = .71183$; $R_{13}^{2} = .42882.$

$$F = \frac{(R_{10}^{2} - R_{13}^{2})/2}{(1 - R_{10}^{2})/(N - 6)} = \frac{.28301/2}{(1 - .71183)/24} = 11.79, p < .01.$$

This F test tests simultaneously $\overline{Y}_2 - \overline{Y}_1 = \overline{Y}_4 - \overline{Y}_3$ and $\overline{Y}_5 = \overline{Y}_6$; placing both sets of restrictions allows the rejection of the null hypotheses. If these restrictions are equivalent to hypotheses the researcher had in mind, then there is no further problem. Translating the meaning of these two hypotheses into English may leave the researcher somewhat uneasy; however, one attempt at a translation into English is: It is not simultaneously true that there is no differences in the means of the non-pretested group and that there is no differences in the gains of the pre-tested groups.

 \cdot

$$R_{15}^2 = .66038$$
 and

$$F = \frac{(R_{10}^2 - R_{15}^2)/1}{(1 - R_{40}^2)/(N-6)} = \frac{.71183 - .66038}{(1 - .71183)/24} = \frac{.05145}{(1 - .71183)/24} = 4.29$$

 $t = \sqrt{F}.= 2.07$. Since two contrasts are planned, a value of 2.39 is necessary for significance of the .05 level, hence the hypothesis $\sqrt{2} - \sqrt{1} = \sqrt{4} - \sqrt{3}$, corresponding to $\sqrt{2} - \sqrt{1} = \sqrt{4} - \sqrt{3}$ cannot be rejected. The imposition of the second restriction $(b_5 = b_6)$ yields:

$$Y = b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 X_4 + b_5 X_5 + b_6 X_6 + e_{12};$$

$$Y = b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 X_4 + b_5 (X_5 + X_6) + e_{12}.$$
Using D_4 , (16)

$$R_{17}^{2} = .48028 \text{ and } F = \frac{(R_{10}^{2} - R_{17}^{2})/1}{(1 - R_{10}^{2})/(N - 6)} = \frac{.71183 - .48028}{(1 - .71183)/24} = \frac{.23155}{(1 - .71883)/24} = 19.28,$$

t = \sqrt{F} = 4.39, t>3.09 from Dunn's table, so that p<.01. Note also that from the numerator of these two tests that .05145 + .23155 = .28300, within rounding error of the numerator when both restrictions were applied; this is because these contrasts are independent. From these calculations, it can be seen that the greatest portion of the rejection of the hypotheses tested by the restrictions in equation 13 is due to the differences in the groups that were posttested only rather than due to differential increases.

A second set of restrictions (actually, a single restriction) is given as $(b_2-b_1)-(b_4-b_3)=b_5-b_6$. This restriction tests the hypothesis related to $(\overline{Y}_2-\overline{Y}_1)-(\overline{Y}_4-\overline{Y}_3)=\overline{Y}_6-\overline{Y}_5$, that is, the difference between the mean of the gain scores is equal to the difference in posttest measures of the non-pretested group. The restriction can be stated as $b_2=b_5-b_6+b_1+b_4-b_3$. Imposing this restriction yields:

$$Y = b_1 X_1 + (b_5 - b_6 + b_1 + b_4 - b_3) X_2 + b_3 X_3 + b_4 X_4 + b_5 X_5 + b_6 X_6 + e_{13}:$$

$$Y = b_1 (X_1 + X_2) + b_3 (X_3 - X_2) + b_4 (X_4 + X_2) + b_5 (X_5 + X_2) + b_6 (X_6 - X_2) + e_{13} (19)$$



Using D_1 , D_2 , D_3 and defining $D_5 = X_5 + X_2$ and $D_6 = X_6 - X_2$, equation 19 can be rewritten as $Y = b_1 D_1 + b_3 D_2 + b_4 D_3 + b_5 D_5 + b_6 D_6 + e_{13}$. (20) $R_{20}^2 = .70326$.

Then
$$F = \frac{(.71183 - .70326)/1}{(1 - .71183)/24} = \frac{.01857}{(1 - .71183)/24} = 1.55,$$

which is non-significant. Thus, while we have previously showed that the differences between the posttested groups is significant (p<.01) and the differences in gains in the pretested groups are non-significant (p>.05), there are no significant differences between the gain of the mean scores and the posttested only groups differences. This is not to say the outcomes for the \$ lomon design are uninterpretable; it does say that the interpretations are tricky.

Viewing the Solomon as a Three-Way Design

It is possible to view the Solomon design as a 2x2x2 design with two missing cells. The missing cells are planned, as was the case in missing cell design described by Williams and Wali (1979). In diagramatic form, the three dimensional case can be seen as:

•	Prete	ested
,	Pre	Post
Experimental	Group 1	Group 2
Control	Group . 3	Group 4 °

Non-Pretested					
Pre	Post				
	Group				
Х	5				
	Group				
Х	. 6				

To test for the experimental-control main effect (A effect), the following restriction can be imposed:

$$b_1 + b_2 + b_5 = b_3 + b_4 + b_6$$
which yields
$$Y = b_2 (x_2 - x_1) + b_3 (x_3 + x_1) + b_4 (x_4 + x_1) + b_5 (x_5 - x_1) + b_6 (x_6 + x_1) + e_{14}.$$
Defining $D_7 = x_2 - x_1$;
$$D_8 = x_3 + x_1$$
;



$$p_9 = x_4 + x_1$$
;

$$D_{10} = X_5 - X_1$$
; and $D_{11} = X_6 + X_1$

$$-Y = b_2 D_7 + b_3 D_8 + b_4 D_9 + b_5 D_{10} + b_6 D_{11} + e_{14}.$$
 (22)

$$R_{22}^2 = .29159;$$

$$F = \frac{(.71183 - .29159)/1}{(1 - .71183)/24} = \frac{.42024}{.28817/24} = 35.00, p<.01.$$

To test the effect of pretesting (the B effect), several rival hypotheses might be used to serve as the main effect.

One such hypothesis is $b_1^{+b}2^{+b}3^{+b}4^{=b}5^{+b}6$. This hypothesis does not test the more appropriate hypothesis of interest, since the pretested scores are being compared to the scores which have been posttested only. More interesting is $b_2^{+b}4^{=b}5^{+b}6$ or $b_2^{=b}5^{+b}6^{-b}4$.

Then.

$$Y = b_{1}X_{1} + b_{3}X_{3} + b_{4}(X_{4} - X_{2}) + b_{5}(X_{5} + X_{2}) + b_{6}(X_{6} + X_{2}) + e_{15}.$$

$$Defining D_{12} = A_{4} - X_{2};$$

$$D_{13} = X_{5} + X_{2};$$

$$D_{14} = X_{6} + X_{2};$$

$$D_{14} = X_{6} + X_{2};$$

$$D_{15} = X_{15} + X_{25};$$

$$D_{16} = X_{15} + X_{15};$$

$$D_{17} = X_{15} + X_{15};$$

$$D_{18} = X_{15} + X_{15} + X_{15};$$

$$D_{18} = X_{15} + X_{15} +$$

$$Y = b_1 X_1 + b_3 X_3 + b_4 D_{12} + b_5 D_{13} + c_6 D_{14} + e_{15}.$$
 (24)

$$R_{24}^2 = .69897;$$

$$F = \frac{(.71183 - .69897)/1}{(1 - .71183)/24} = \frac{.01286}{(1 - .71183)/24} = 1.07, p>.05.$$

The outcome of this test would suggest that the effect of pretesting per se is minimal for this data set.

To test for pre-post differences (the C main effect), the restriction $b_1 + b_3 = b_2 + b_4$ or $b_1 + b_3 = b_2 + b_4$ or $b_1 + b_3 = b_2 + b_4$ or $b_1 + b_3 = b_3 + b_4 + b_5 = b_3 + b_4 + b_5 = b_3 + b_4 + b_5 + b_5 + b_6 = b_6 + b_6 + b_6 = b_6 + b_6 + b_6 = b_6 + b_6 + b_6 + b_6 + b_6 = b_6 + b_6$

Letting $D_{15} = X_3 - X_1$, equation 25 can be rewritten $Y = b_2 D_1 + b_3 D_{15} + b_4 D_9 + b_5 X_5 + b_6 X_6 + e_{16}.$ (26) $R_{26}^2 = .50600;$ $F = \frac{(.71183 - .50600)/1}{(1 - .71183)/24} = \frac{.20583}{(1 - .71183)/24} = 17.14, p < .01.$

indicating a pre-test increase in scores.

Interactions in the Three-Way Design

First of all, the two missing cells will cause the non-existence of two interactions. The three way interaction will not exist, since it is impossible to have non-pretested groups who were pretested. For the same reason, the BC interaction will fail to exist. To test for the AB interaction, that is, the interaction between the experimental-control condition (A) and the effect of pretesting (B), the restriction on the full model would be: $b_2 - b_5 = b_4 - b_6 \text{ or } b_2 = b_4 - b_6 + b_5.$ Then $Y = b_1 X_1 + (b_4 - b_6 + b_5) X_2 + b_3 X_3 + b_4 X_4 + b_5 X_5 + b_6 X_6 + e_1 T$, or $Y = b_1 X_1 + b_3 X_3 + b_4 (X_4 + X_2) + b_5 (X_5 + X_2) + b_6 (X_6 - X_2) + e_1 T$. (27)

Using previously defined transformations, Y = $b_1 X_1 + b_3 X_3 + b_4 D_3 + b_5 D_{13} + b_6 D_6 + e_{17}$. (28) R_{17}^2 = .71183; R_{17}^2 is identical to the R^2 for the full model. This is circumstantially so because $\overline{Y}_2 - \overline{Y}_5 = \overline{Y}_4 - \overline{Y}_6 = 13 - 12 = 7 - 6$. Thus, the AB interaction is equal to zero.

To test the AC interaction, that is, the experimental-control condition (A) with pre-post differences (C), the restriction b_2 - b_1 = b_4 - b_3 would be imposed on the full model. This in fact was already done in equation 15, yielding R_{15}^2 =.66038, F = 4.29, p>.05. The results from the three-way analysis can be placed into a symmary table; see Table 4:

Table 4
Summary Table for a Three-Way Solution to the Solomon Design

' Effect	Restriction	R^2	df	SS	MS	F
F.11 Model A (experimental-control)	b ₁ +b ₂ +b ₅ =b ₃ +b ₄ +b ₆	.29159	1	163.33	163.33	35.00
B (pretesting)	b2+b4=b5+b6	.69897	1	5.00	5.00	1.07
C (pre-post differences)	b ₁ +t ₃ =b ₂ +b ₄	.50600	1	80.00	80.00	17.14
AB	b2-t5=b4-b6	.71183	l	0	0	0
AC	b ₂ -b ₁ =b ₄ -b ₃	.66038	1	20.00	20.00	4.29
Deviation from Full Model		.28817	24	112.00	4.67	

Finding the sum of squares in Table 4 is facilitated by knowing $SS_T = 388.67$. Also, the C effect and the AC effect are identical to the same effects as shown in Table 3.

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